



p-hacking strategies

Presenter: Bui Minh Tri



Objective + Outline



- Objective

p-hacking strategies

- Outline

1. Selective reporting DV

2. Selective reporting IV



Introduction



p-hacking



- Compound strategies: non-significant \Rightarrow significant result.
- Not every researcher aware of it.
 - **Not necessarily an intentional attempt at gaming the system.**



1. Selective reporting dependent variable



Background



- **p-hacking:**
 - ✓ Treatment vs control group: compare different outcome/ dependent variables.

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Independent

Table 1b | Efficacy of surgical face masks in reducing respiratory virus frequency of detection and viral shedding in respiratory droplets and aerosols of symptomatic individuals with coronavirus, influenza virus or rhinovirus infection

Virus type	Droplet particles > 5 μm			Aerosol particles ≤ 5 μm		
	Without surgical face mask	With surgical face mask	P	Without surgical face mask	With surgical face mask	P
Detection of virus						
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Rhinovirus	9 of 32 (28)	6 of 27 (22)	0.77	19 of 34 (56)	12 of 32 (38)	0.15
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Leung NH, Chu DK, Shiu EY, Chan KH, McDevitt JJ, Hau BJ, Yen HL, Li Y, Ip DK, Peiris JS, Seto WH. Respiratory virus shedding in exhaled breath and efficacy of face masks. Nature medicine. 2020 May;26(5):676-80.

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- ✓ Conduct 1 hypothesis test for each dependent variable.

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Background



- **p-hacking:**
 - ✓ Treatment vs control group: compare different outcome/ dependent variables.
 - ✓ Conduct 1 hypothesis test for each dependent variable.
 - ✓ Selectively report the significant results.



1. Selective reporting the dependent variable



- Assume using t-test.
- **FPR from 3 – 10 dependent variables ?**



1. Selective reporting the dependent variable

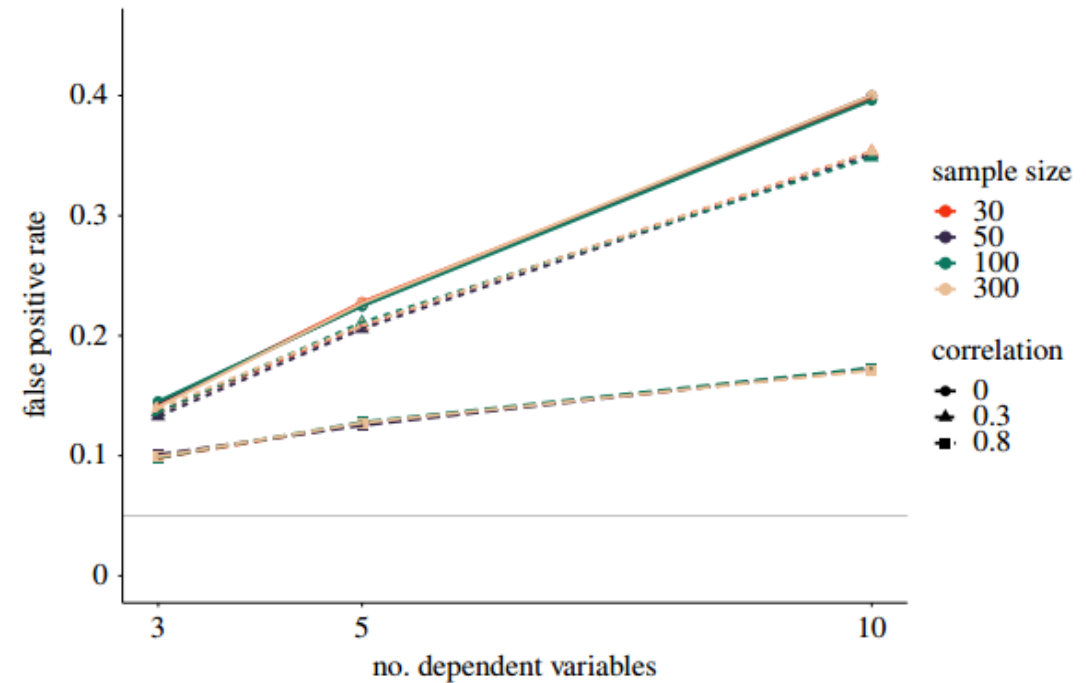


- Assume using t-test.
- **FPR from 3 – 10 dependent variables ?**

	Virus Type	Without mask	With mask	p
1	Coronavirus	0.3 (0.3, 1.2)	0.3 (0.3, 0.3)	0.07
2	Influenza virus	0.3 (0.3, 1.1)	0.3 (0.3, 0.3)	0.01
...
10	Rhino virus	0.3 (0.3, 1.3)	0.3 (0.3, 0.3)	0.44

1. Selective reporting the dependent variable

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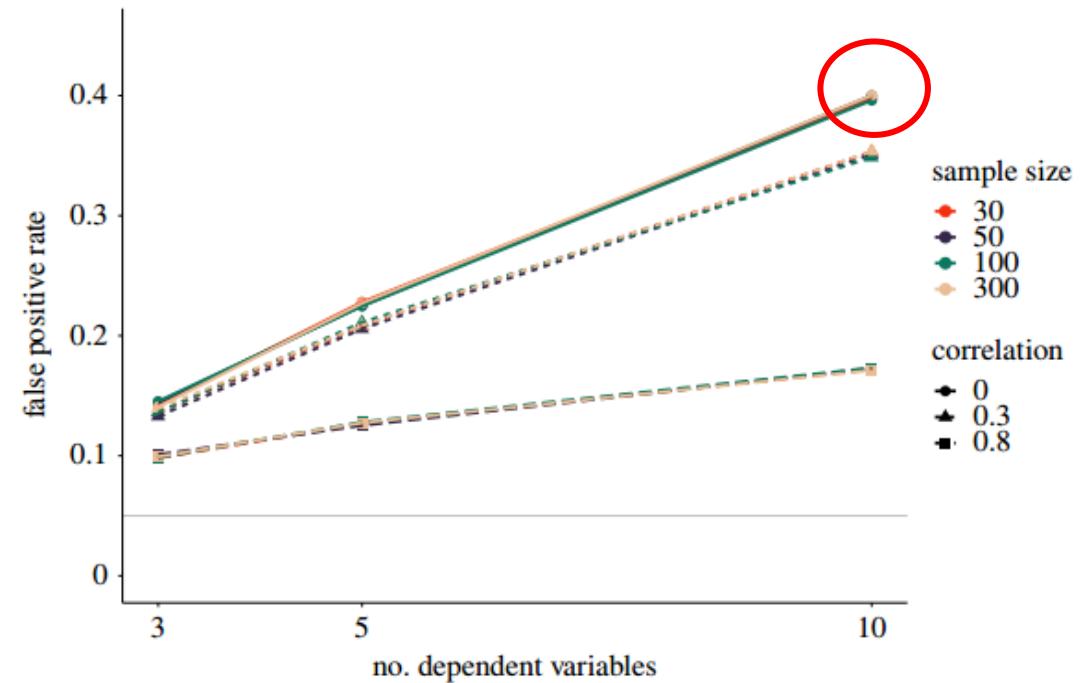


Number of dependent variables indicates how many hypothesis tests were conducted (at maximum) to obtain a significant result.

The solid grey line: nominal α -level of 5%.

1. Selective reporting the dependent variable

- Assume using t-test.
- Sample size: not a protective factor.
- 10 variables – **correlation = 0**: FPR \approx 40%

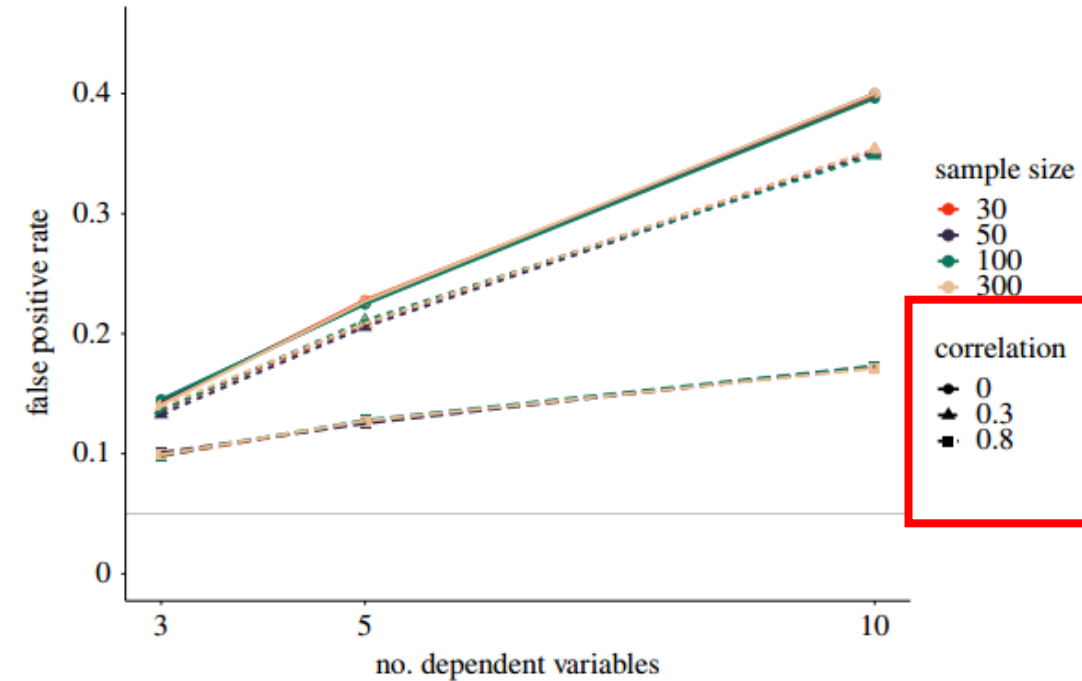
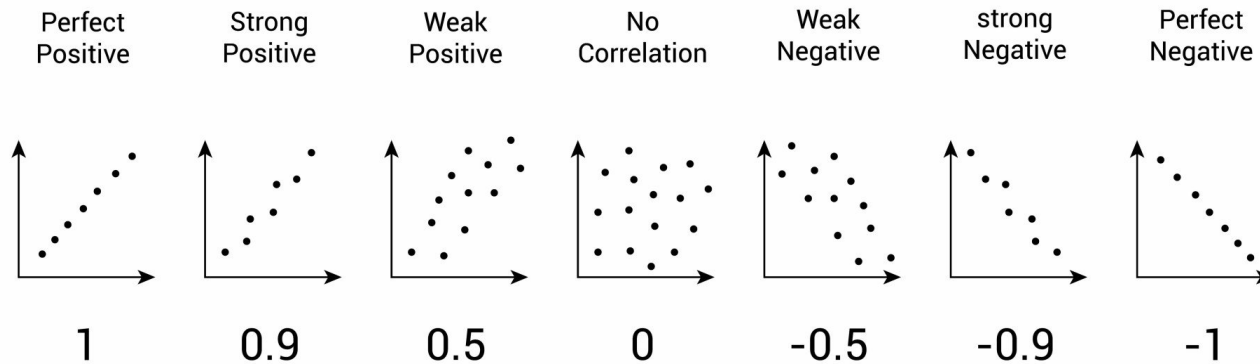


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What is correlation ?

- Relationship **2 quantitative variables**
- Correlation coefficient (r)**



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What is correlation ?

	Case N=503	Control N=493	p value
Height	158 [153;165]	158 [154;165]	0.662
Weight	62.0 [55.0;70.0]	58.0 [52.8;65.0]	<0.001
BMI	24.3 [22.4;27.2]	23.2 [21.1;25.4]	<0.001
Waist	86.0 [80.0;93.0]	82.0 [75.0;88.0]	<0.001
Hip	95.0 [89.0;100]	92.0 [86.0;97.0]	<0.001

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Correlation Test

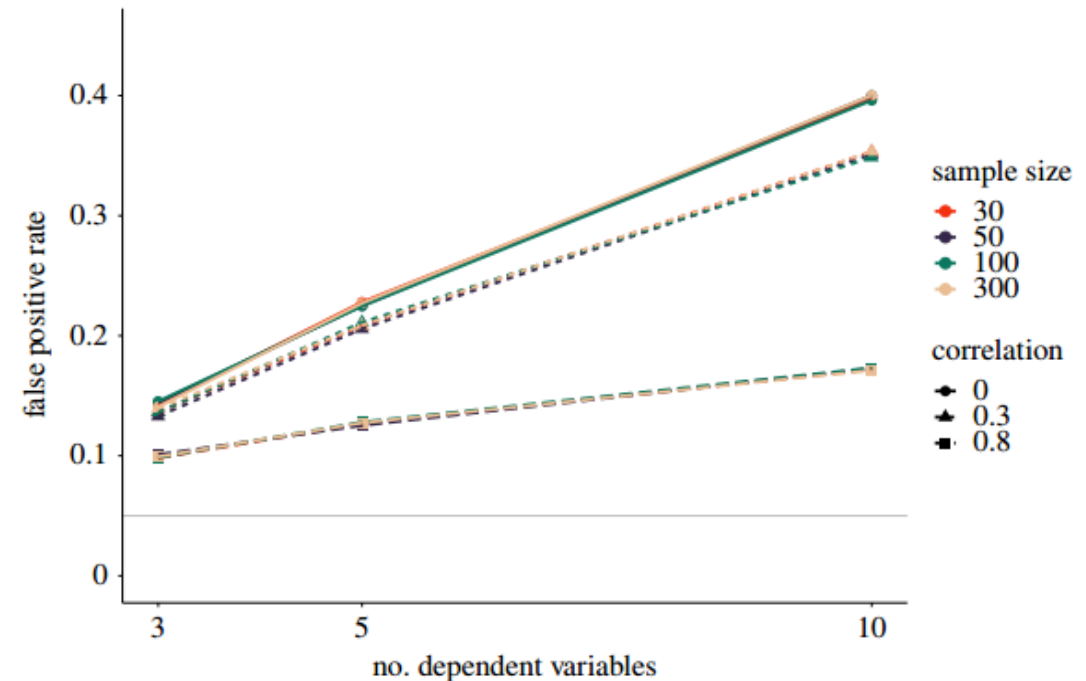
Correlation coefficient (r)

	height	weight	BMI	waist	hip
height	1.00	0.51	-0.02	0.20	0.19
weight	0.51	1.00	0.82	0.76	0.70
BMI	-0.02	0.82	1.00	0.77	0.70
waist	0.20	0.76	0.77	1.00	0.77
hip	0.19	0.70	0.70	0.77	1.00

P	height	weight	BMI	waist	hip
height		0.0000	0.5275	0.0000	0.0000
weight	0.0000		0.0000	0.0000	0.0000
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1. Selective reporting the dependent variable

- Assume using t-test.
- Sample size: not a protective factor.
- 10 variables – **correlation = 0**: FPR \approx 40%
- **FPR decreases** with:
 - ✓ **Less dependent variables.**
 - ✓ **Higher correlations variables**



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Multiple testing issue



- **Question:** \uparrow hypothesis tests \Rightarrow \uparrow False Positive Rate ?

- If perform **m hypothesis independent tests**, **the probability at least 1 false positive** ?

✓ P (Making Type I error)	= α
✓ P (Not making Type I error)	= $1 - \alpha$
✓ P (Not making an error in m tests)	= $(1 - \alpha)^m$
✓ P (Making at least 1 error in m tests)	= $1 - (1 - \alpha)^m$

- Example: $m = 100$ tests, $\alpha = 0.05 \Rightarrow P = 1 - (1 - 0.05)^{100} = 0.99$

➤ If have 100 hypothesis tests, the probability at least 1 false positive: 99%

Multiple testing issue

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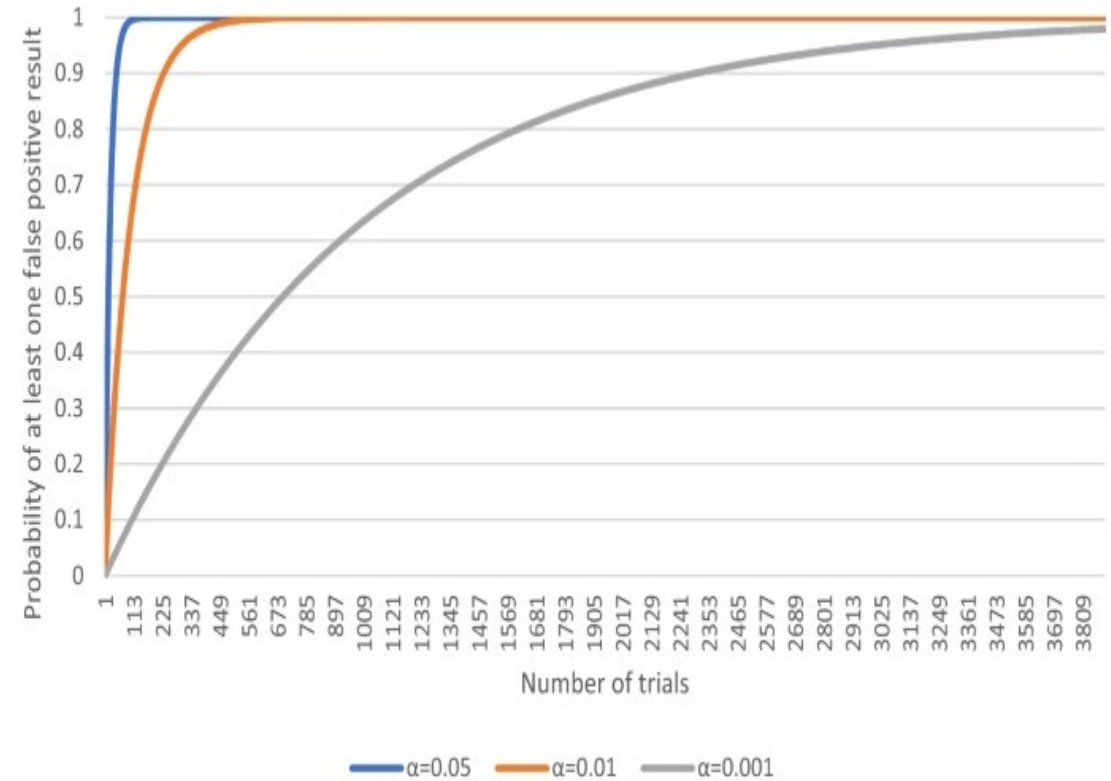
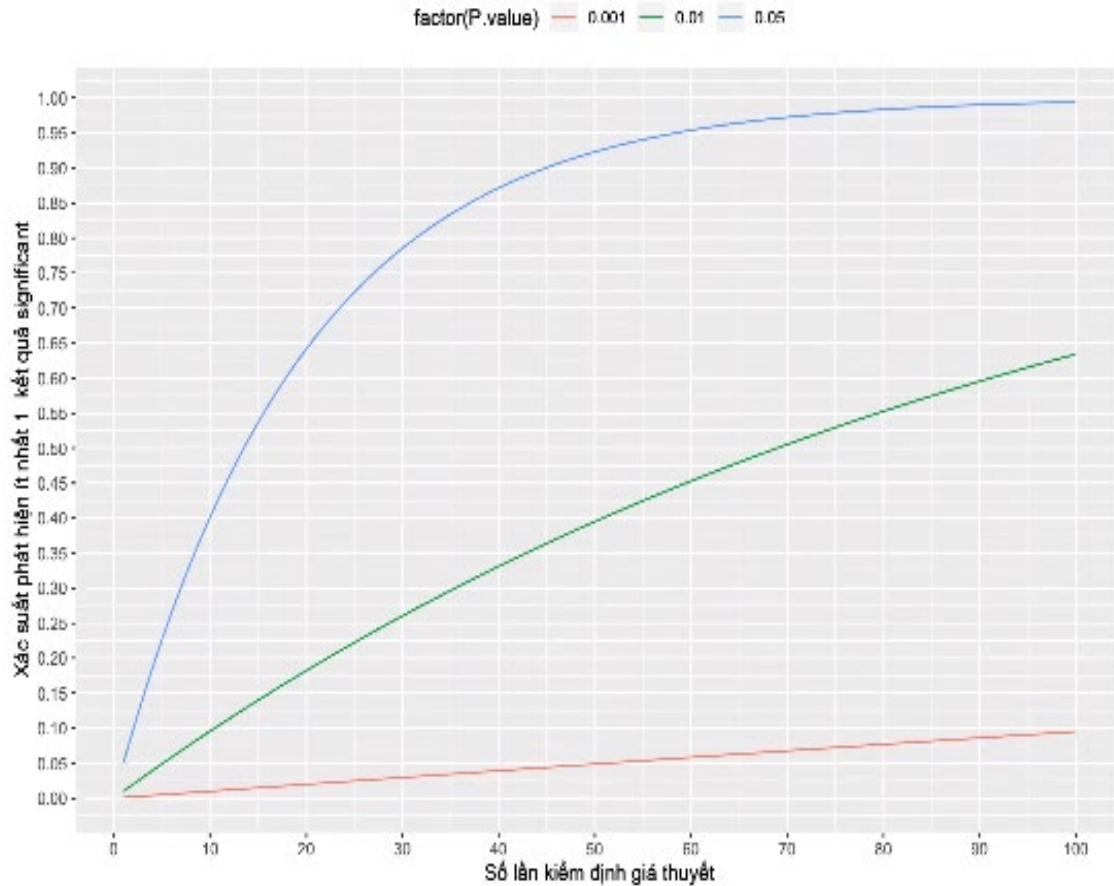
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$$\begin{aligned}
 P(\text{Making at least 1 error in } m \text{ tests}) &= 1 - (1 - \alpha)^m \\
 &= 1 - (1 - 0.05)^{12} = 0.4596 = 45.96\%
 \end{aligned}$$

Leung NH, Chu DK, Shiu EY, Chan KH, McDevitt JJ, Hau BJ, Yen HL, Li Y, Ip DK, Peiris JS, Seto WH. Respiratory virus shedding in exhaled breath and efficacy of face masks. *Nature medicine*. 2020 May;26(5):676-80.

Multiple testing issue



The probability of obtaining at least one false positive result $P(FP \geq 1)$ (own calculation)

NguyenVanTuan-
<https://www.youtube.com/watch?v=RPjVPHpeu2o&t=2517s>

Maziarz M, Stencel A. The failure of drug repurposing for COVID-19 as an effect of excessive hypothesis testing and weak mechanistic evidence. History and Philosophy of the Life Sciences. 2022 Dec;44(4):47.



Bonferroni Correction



- Bonferroni correction: $\alpha^* = \alpha / m$
 - ✓ α : significance level.
 - ✓ m : number of hypothesis tests.



Bonferroni Correction



- Bonferroni correction: $\alpha^* = \alpha / m$
 - ✓ α : significance level.
 - ✓ m : number of hypothesis tests.

 - Example: Bonferroni to test 3 hypotheses with p :
 - ✓ **H1: $p = 0.01$**
 - ✓ H2: $p = 0.02$
 - ✓ H3: $p = 0.03$
 - $\alpha^* = \alpha / m = 0.05 / 3 = 0.0167$
- => We'd need $p \leq 0.0167$ to declare significance.

Bonferroni Correction

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$$\alpha^* = \alpha / m = 0.05 / 12 = 0.004$$

=> We'd need $p \leq 0.004$ to declare significance.

- “No adjustments for multiple comparisons were made”.

Google Scholar search results for "No adjustments for multiple comparisons were made" - breast cancer. The search returned about 24 results in 0.04 seconds.

Articles About 24 results (0.04 sec)

Any time
Since 2024
Since 2023
Since 2020
Custom range...

Sort by relevance
Sort by date

Any type
Review articles

include patents
 include citations

Create alert

Psychological measures of stress and biomarkers of inflammation, aging, and endothelial dysfunction in breast cancer survivors on aromatase inhibitors [PDF] nature.com
AH Blaes, C Nair, S Everson-Rose, P Jewett, J Wolf... - Scientific reports, 2023 - nature.com
... with **breast cancer** in their lifetime. Although **breast cancer** is a leading cause of **cancer** ...
No adjustments for multiple comparisons were made. All analyses were conducted using R ...
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Factors associated with weight gain in pre-and post-menopausal women receiving adjuvant endocrine therapy for breast cancer [PDF] springer.com
ACR Uhelski, AL Blackford, JY Sheng, C Snyder... - Journal of Cancer ..., 2023 - Springer
... The findings presented here are for descriptive purposes and **no adjustments for multiple comparisons were made.** Analyses were performed with R version 4.0.3 [88]. ...
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Effect of an educational intervention on women's health care provider knowledge gaps about breast cancer risk model use and high-risk screening recommendations
RL Seitzman, JA Pushkin, WA Berg - Journal of Breast Imaging, 2023 - academic.oup.com
... Gail model predicts lifetime invasive **breast cancer** risk; this ...) to predict lifetime invasive **breast cancer** risk. These knowledge ... **No adjustments for multiple comparisons were made** (27). ...
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A pilot study of Neoadjuvant Nivolumab, Ipilimumab, and Intralesional Oncolytic Virotherapy for Her2-negative breast cancer [PDF] aacrjournals.org
VP Nguven, KM Campbell, TS Nowicki... - Cancer Research ..., 2023 - AACR



microRNA-145-5p inhibits prostate cancer bone metastatic by modulating the epithelial-mesenchymal transition

Bingfeng Luo^{1†}, Yuan Yuan^{1†}, Yifei Zhu¹, Songwu Liang¹, Runan Dong¹, Jian Hou¹, Ping Li², Yaping Xing¹, Zhenquan Lu¹, Richard Lo¹ and Guan-Ming Kuang^{3*}

¹Division of Urology, Department of Surgery, The University of Hong Kong-Shenzhen Hospital, Shenzhen, China, ²Department of Pathology, The University of Hong Kong-Shenzhen Hospital, Shenzhen, China, ³Department of Orthopedics and Traumatology, The University of Hong Kong-Shenzhen Hospital, Shenzhen, China



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[†]These authors have contributed equally to this work

SPECIALTY SECTION
This article was submitted to

incubation for 1 h. For the migration/wound healing assays, 3×10^5 cells/well were grown in a 24-well plate, incubated for 16-18 h and cell monolayers scraped with a pipette tip to create a wound which was washed with PBS. After incubation for 24 h in culture medium, an inverted microscope with a digital camera was used to photograph wound closure. Colony formation was measured by resuspending the cells with 1ml medium and seeding a six-well plate with 500 cells per well. After 2 weeks, 6-well plates were fixed with paraformaldehyde (4%) for 30min at room temperature before washing with PBS, the addition of crystal violet staining and photographs taken under the microscope. Transwell assay was conducted to assess invasion.

TBS, proteins were visualized with an electroluminescence kit (ASPEN, Wuhan, China). The internal control was GAPDH.

Statistical analysis

Means \pm SD of three independent experiments were presented, and statistical analysis was conducted using GraphPad v4.1 (CA, USA). Data were compared between groups using a two-tailed unpaired Student's t-test. A p-value of <0.05 was deemed statistically significant.



In article



Statistical analysis

Statistical analyses were performed using Pearson's Chi-squared test or Fisher's exact test to determine significant clinicopathological differences between EGFR expression in positive and negative tumors, between EGFR FISH-positive and FISH-negative tumors, and between tumors with and without EGFR mutations. These tests were also used to determine the association between EGFR protein expression, EGFR FISH results, and EGFR mutations. **Bonferroni correction** was performed to adjust for multiple comparisons, differences with $P < 0.05/\text{comparison times}$ were considered significant.

EGFR mutations in lung adenocarcinomas

Eighty-five (63.9%) of the 133 cases showed EGFR mutations, which included 2 exon 18 G719X mutations (one also had an exon 20 S768I mutation), 39 exon 19 deletions, 4 exon 20 insertion mutations, 3 exon 20 S768I mutations (one also had an exon 18 G719X mutation), 35 exon 21 L858R mutations (one also had an exon 20 T790 M mutations), and 3 exon 21 L861Q mutation. After **Bonferroni correction** for 5 comparisons, $P < 0.01$ were considered significant, EGFR mutations were significantly associated with smoking status (non-smoking vs. smoking, $p = 0.008$), and were not associated with age, gender, lymph node metastasis or tumor stage ($p \geq 0.01$) (Table [1](#)).

Liang Z, Zhang J, Zeng X, Gao J, Wu S, Liu T. Relationship between EGFR expression, copy number and mutation in lung adenocarcinomas. BMC cancer. 2010 Dec;10:1-9.



2. Selective reporting independent variable



Background



- **p-hacking:**

- ✓ Multiple experimental groups vs 1 control group.

- Example: Different Drug vs Control

Different Drug Concentrations vs Control

- ✓ Compares all experimental groups to the control group.

- ✓ Only report the significant results.

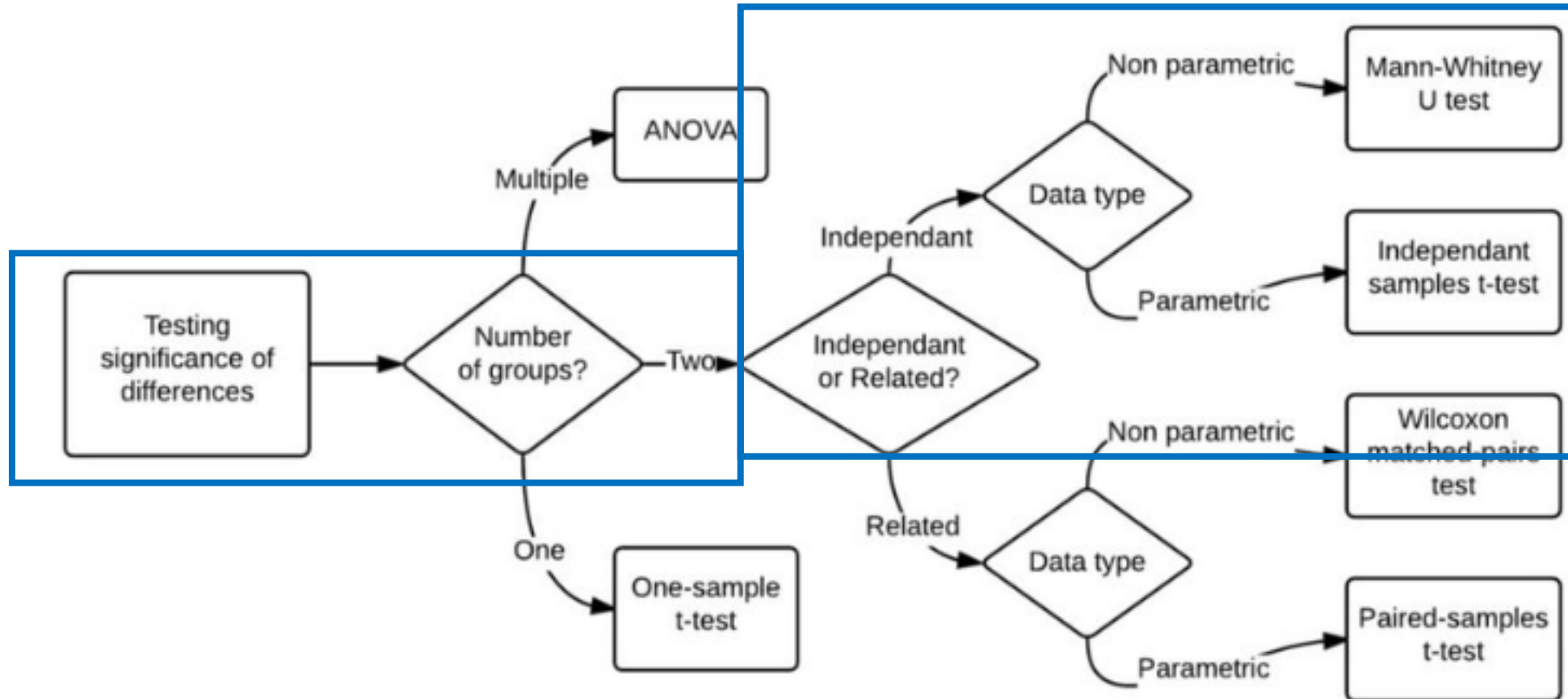


Background



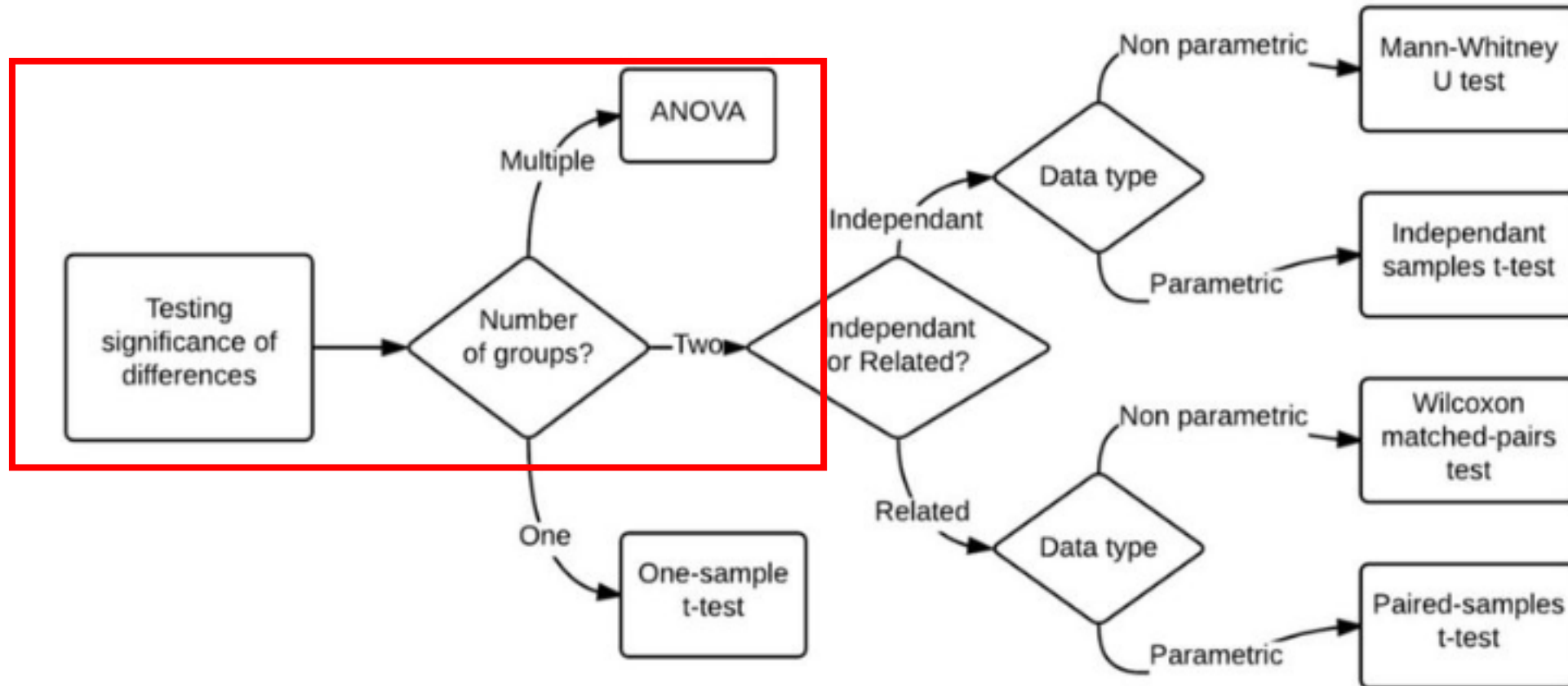
<i>Control</i>	<i>Drug 1</i>	<i>Drug 2</i>
1147	1169	1009
1273	1323	1260
1216	1276	1143
1046	1240	1099
1108	1432	1385
1265	1562	1164

Lew M. Good statistical practice in pharmacology Problem 2. British journal of pharmacology. 2007 Oct;152(3):299-303.



Statistical analysis decision tree for testing significance of differences

Borghini YC. *An Assessment and Learning Analytics Engine for Games-based Learning* (Doctoral dissertation, University of the West of Scotland).



Statistical analysis decision tree for testing significance of differences

Borghini YC. *An Assessment and Learning Analytics Engine for Games-based Learning* (Doctoral dissertation, University of the West of Scotland).

t-test vs ANOVA

		Independent t-test	ANOVA
Null Hypothesis		No difference between population's means. Ho: $\mu_1 = \mu_2$	No difference between population's means. Ho: $\mu_1 = \dots = \mu_k$
Alternative hypothesis		Difference between 2 populations' means. H1: $\mu_1 \neq \mu_2$	At least 2 group means are different from each other. H1: $\mu_1 \neq \mu_2$ or $\mu_1 \neq \mu_3$ or $\mu_2 \neq \mu_3$
Conclusion	$p > 0.05$	We don't have enough evidence to conclude that the difference is statistically significant.	We don't have enough evidence to conclude that the difference is statistically significant.
	$p \leq 0.05$	We have enough evidence to conclude that the difference is statistically significant.	There is a significant effect of independent variable on levels of / according to response variable.



t-test vs ANOVA



- After perform hypothesis test:
 - ✓ **Independent t-test** \Rightarrow Conclusion 2 groups
 - ✓ **ANOVA** \Rightarrow Which groups differ ??
- **Post Hoc Tests for ANOVA**
 - ✓ 1 vs 2
 - ✓ 1 vs 3
 - ✓ ...
 - ✓ m vs n

- Multiple testing issue: P (At least 1 error in m tests) = $1 - (1 - \alpha)^m$
- 2 approaches:

✓ Compare $p \leq \alpha^*$

$$\alpha^* = \alpha / m = 0.05 / 3 = 0.017.$$

✓ Compare $p^* \leq \alpha$

$$p^* = p * m = p * 3$$

```

Bonferroni
-----
Pairwise comparisons using t
tests with pooled SD

data:  viagraData$libido and
viagraData$dose

           Placebo Low Dose
Low Dose  0.845    -
High Dose 0.025  0.196

P value adjustment method:
bonferroni
  
```

```

BH
-----
Pairwise comparisons using t
tests with pooled SD

data:  viagraData$libido and
viagraData$dose

           Placebo Low Dose
Low Dose  0.282    -
High Dose 0.025  0.098

P value adjustment method: BH
  
```

```

Tukey multiple comparisons of means
95% family-wise confidence level

Fit: aov(formula = libido ~ dose, data = viagraData)

$dose
      diff      lwr      upr    p adj
Low Dose-Placebo  1.0 -1.3662412  3.366241 0.5162761
High Dose-Placebo  2.8  0.4337588  5.166241 0.0209244
High Dose-Low Dose  1.8 -0.5662412  4.166241 0.1474576
  
```



Background



ANOVA

Control	Drug 1	Drug 2
1147	1169	1100
1273	1323	1125
...
1108	1276	1110
1265	1240	1000

t-test

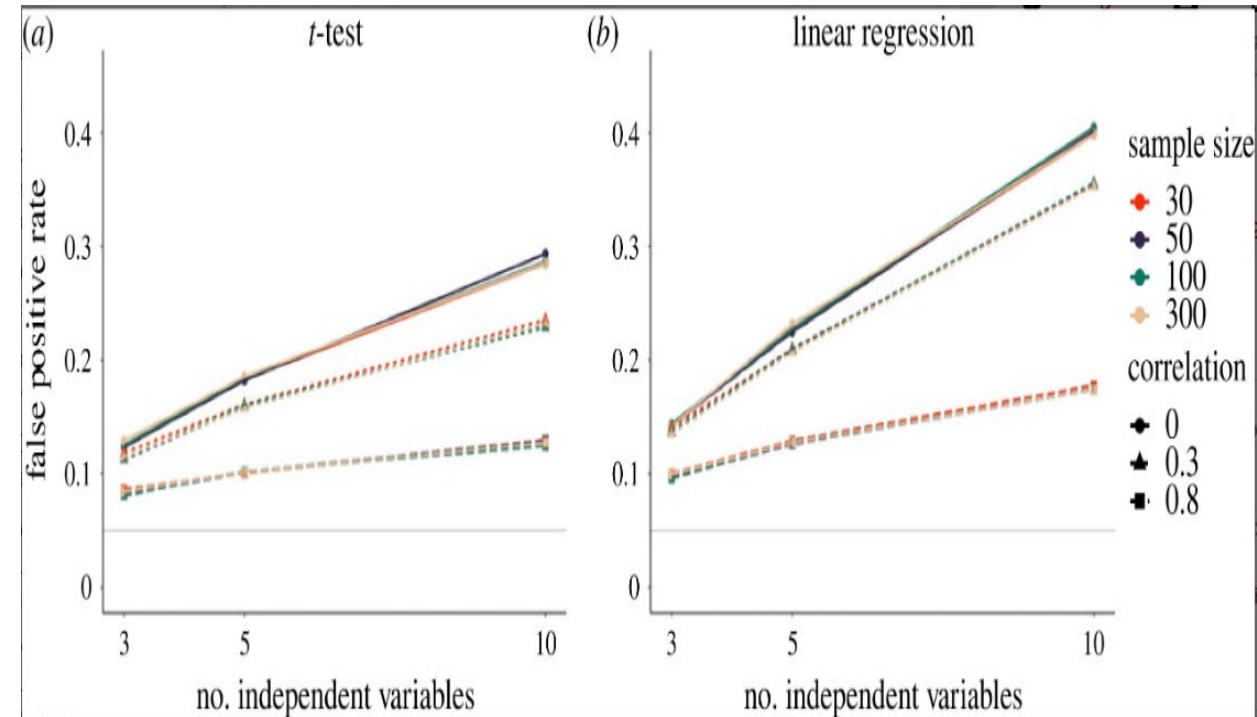


Control	Drug 1
1147	1169
...	...
1265	1240

Control	Drug 2
1147	1100
...	...
1265	1000

2. Selective reporting the independent variable

- Assume using t-test.
- Sample size: not a protective factor.
- **FPR decrease** with:
 - ✓ **Less independent variables.**
 - ✓ **Higher correlation variables.**
- Severe effects in regression \gg t-tests.



Number of independent variables indicates how many hypothesis tests were conducted (at maximum) to obtain a significant result.

The solid grey line: nominal α -level of 5%.

(a) FPR for the *t*-test.

(b) FPR for a univariate regression.



Conclusion



- Selective reporting DV
 - ✓ What is correlation
 - ✓ Multiple testing hypothesis issue

- Selective reporting IV
 - ✓ Post Hoc Tests for ANOVA



References



1. Stefan AM, Schönbrodt FD. Big little lies: A compendium and simulation of p-hacking strategies. Royal Society Open Science. 2023 Feb 8;10(2):220346.



Thank you for listening